

MODEL SELECTION FOR MR STUDIES OF STROKE

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Acute Stroke Chronic Stroke MR, PET & Analysis

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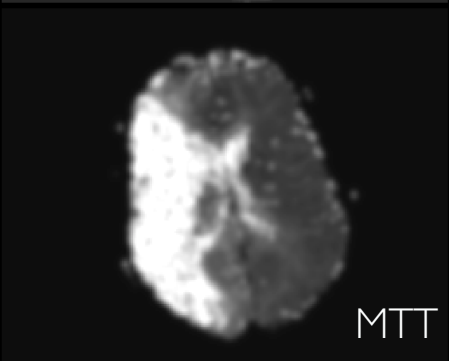
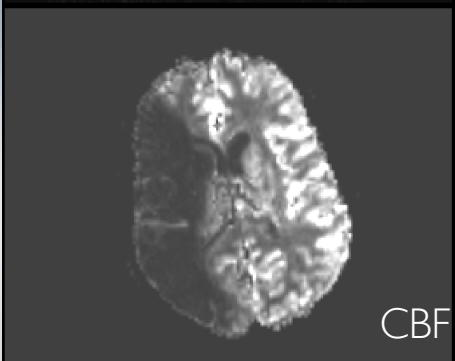
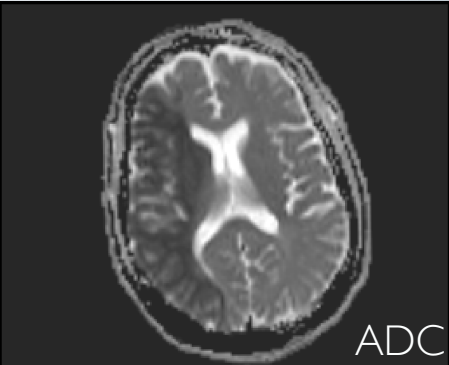
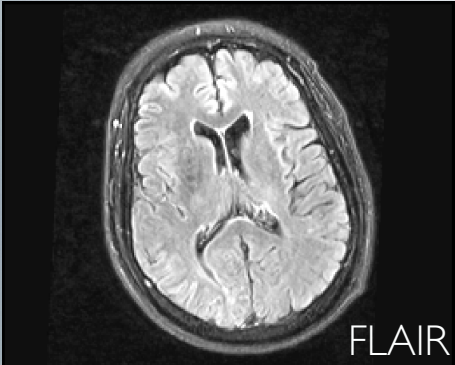
CASE 046

53 YO male arrives in ER at 17:50 by ambulance with L-sided flaccid paralysis, slurred speech, deviation of eyes to right, perseveration. Wife found him lying on floor at 17:30. Patient spoke normally with son at 17:00.

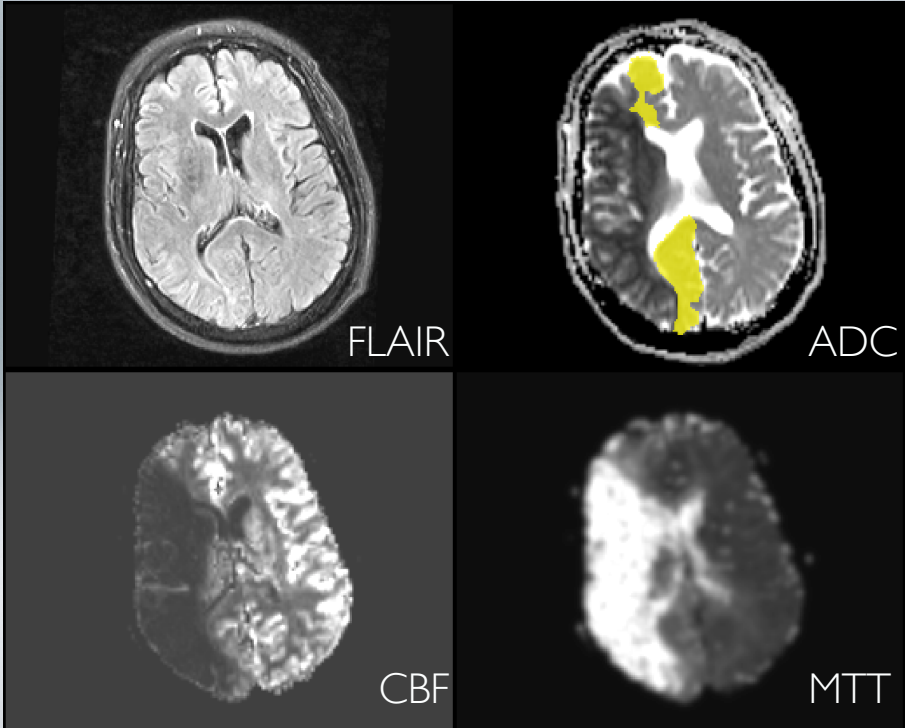
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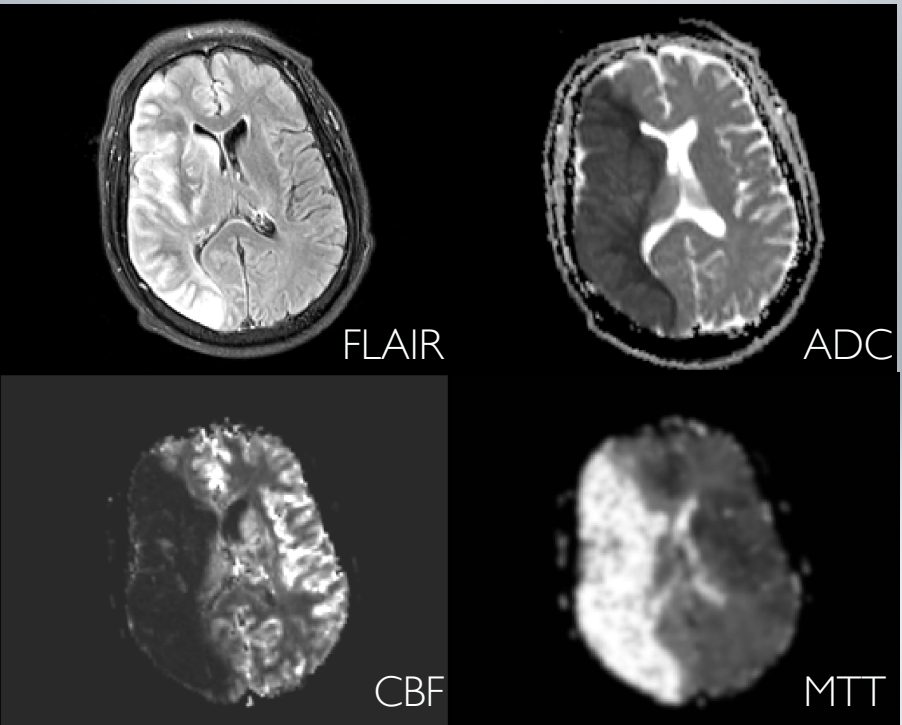
3 HRS



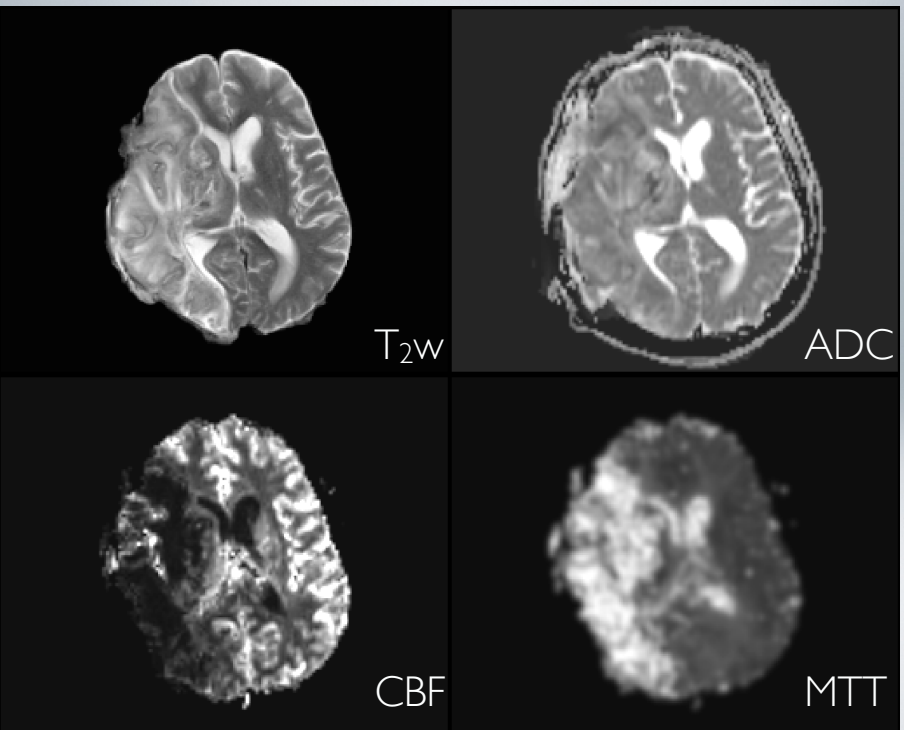
3 HRS



24 HRS



30 DAYS

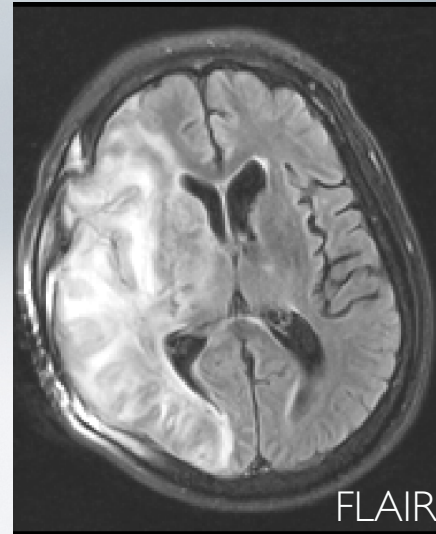


DISCHARGE SUMMARY

Discharged to rehab. 28 days after admission.

Hospital course:

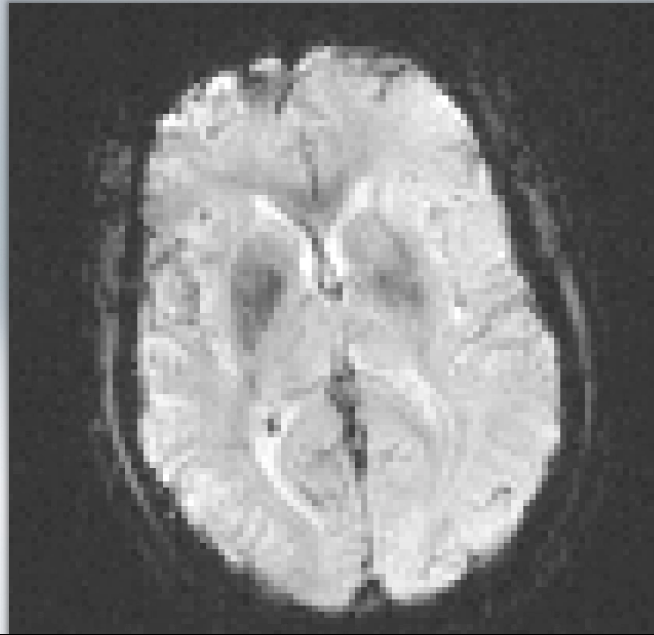
massive stroke + edema.
Received tPA.
Admitted to NNICU.
Intubated.
Craniectomy x2. Coma.
DNR/DNI per family.
Gradually improved &
extubated. Pneumonia.
Remaining dense hemiplegia,
hemi-sensory loss,
L homonymous hemianopsia.



CLINICAL TRIALS

MR perfusion & penumbra estimates have no predictive value for clinical outcomes

EPI, Gd @ 5mL/s



ORGAN PERFUSION

Traditional model for circulating tracer, gamma variate:

$$C_{\vec{r}}(t) \sim \frac{1}{\beta_{\vec{r}}^{\alpha_{\vec{r}}+1} \Gamma(\alpha_{\vec{r}} + 1)} (t - t_{\vec{r},0})^{\alpha_{\vec{r}}} e^{-\beta_{\vec{r}}(t - t_{\vec{r},0})}$$

Diagram illustrating the traditional model for circulating tracer, gamma variate, with annotations:

- $C_{\vec{r}}(t)$: tracer conc.
- t : time sample
- $\vec{r}$: voxel position
- $\beta_{\vec{r}}^{\alpha_{\vec{r}}+1} \Gamma(\alpha_{\vec{r}} + 1)$: Euler's Gamma
- $t_{\vec{r},0}$: arrival time
- $\alpha_{\vec{r}}$: structure/dynamics
- $e^{-\beta_{\vec{r}}(t - t_{\vec{r},0})}$: damping

“Good” agreement with experiments (best available)

Thompson, Circ. Res. 14:503-515 (1964).

Davenport, Nuclear Med., 24:945-948 (1983).

PERFUSION PER VOXEL

Observed tracer concentration $\bar{C}$ comprises:

*unknown scaling:
vascular geometry,
tortuosity,
variable hematocrit*

time sample

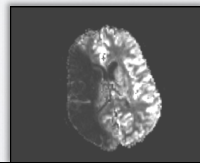
"residue function"

$$\bar{\kappa} C_{\vec{r}}(t) = F_{\vec{r}} R_{\vec{r}}(t) \otimes C_{\vec{r},a}(t)$$

voxel position

cerebral blood flow

tracer conc., arterial supply



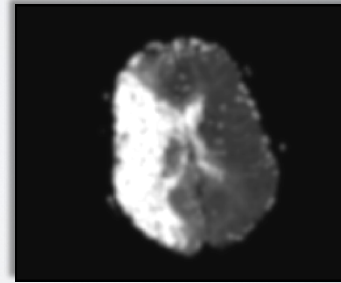
PERFUSION PER VOXEL

Other common perfusion metrics:

Cerebral blood volume (fraction):

$$V_{\vec{r}} = \int^{\infty} dt' C_{\vec{r}}(t') / \int^{\infty} dt' C_{\vec{r},a}(t')$$

Mean transit time: $T_{\vec{r}} \equiv V_{\vec{r}} / F_{\vec{r}}$, viz.



MR

- **Physically:** Bloch equations with fluid dynamics terms (*Torrey, Phys. Rev. 104:563-565 (1956)*)
- Impractical for non-Newtonian, pulsatile flow of blood through “disordered” arterial, capillary & venous networks
- **N.B.:** upon oxygen-extraction in capillary beds, hemoglobin becomes paramagnetic
- **Traditionally:** assume intrinsic T_1, T_2 dynamics may be factored, leaving stationary relaxivity near the bolus passage of Gd:

$$\frac{\|M_{\vec{r}}(t)\|}{\int^{t_{\vec{r}},0} dt' M_{\vec{r}}(t')} \approx \exp \left[- \int^t dt' \mathcal{R}_{\vec{r}}(t') \right] = \exp \left[- \tilde{\mathcal{R}}_{\vec{r}} \int^t dt' C_{\vec{r}}(t') \right]$$

QUESTIONABLE ASSUMPTIONS

- Arterial supply estimated from average of major arterial branches: $C_{\vec{r},a}(t) \implies \overline{C_a(t)}$
- $F_{\vec{r}}, R_{\vec{r}}(t), V_{\vec{r}}$ estimated from SVD of convolution with averaged arterial supply $\overline{C_a(t)}$ using singular value thresholds $\sim 20\%$
- Tracer conc. estimated from: $\log \|M_{\vec{r}}(t)\|$
- Not needed by Bayesian inference...

Inverse
Problems

BAYESIAN ANALYSIS

Gamma-variate: $\mathcal{G}_{\vec{r}}(\alpha, \beta, t_0, t) \equiv \left[\frac{1}{\beta^{\alpha+1} \Gamma(\alpha+1)} (t - t_0)^\alpha e^{-\beta(t-t_0)} \right]_{\vec{r}}$

Residue func.: $R_{\vec{r}}(t) \approx e^{-t/T_{\vec{r}}} \left[\sum_{m=0} c_{\vec{r},m} \left(\frac{t}{T_{\vec{r}}} \right)^m \right] \xrightarrow{\text{model sel.}} e^{-t/T_{\vec{r}}}$

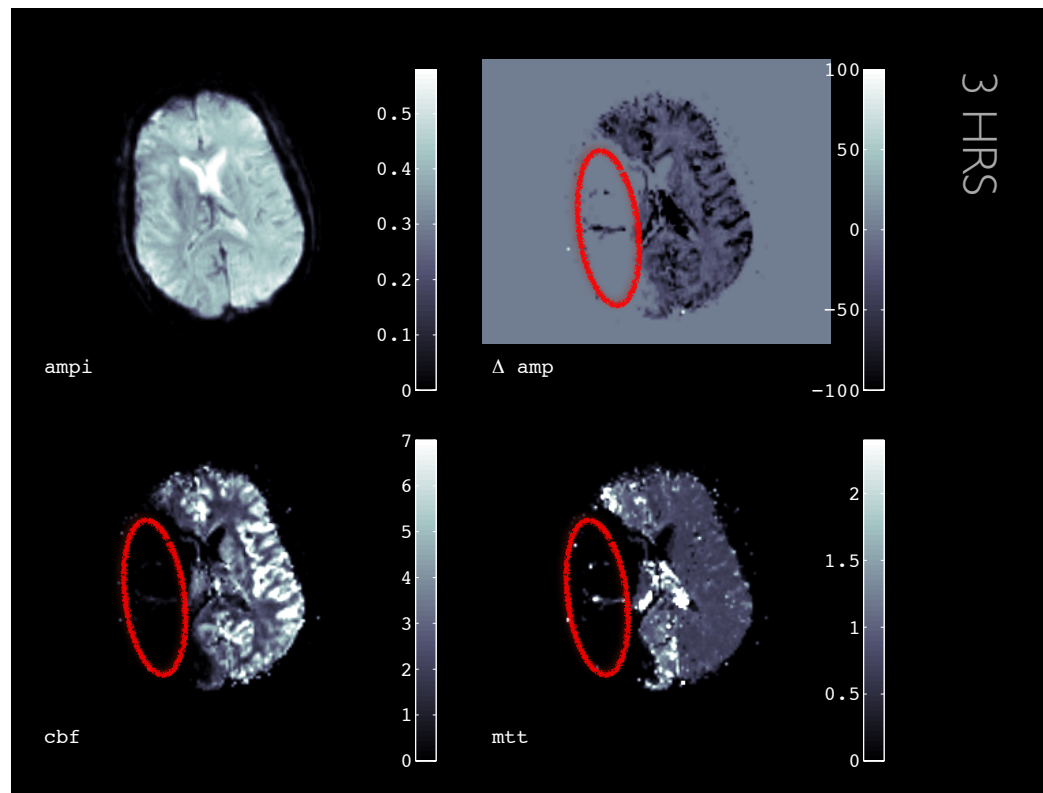
Forward Problem:
$$\frac{\|M_{\vec{r}}(t)\|}{\int_{t_{\vec{r},0}}^t dt' M_{\vec{r}}(t')} \approx \exp \left[-\bar{\kappa} \tilde{\mathcal{H}}_{\vec{r}} \int_{t_{\vec{r},0}}^t dt' \int_{t_{\vec{r},0}}^{t'} dt'' \dots \right. \\ \left. \dots \sum_{\substack{n=0 \\ \text{model sel.}}} F_{\vec{r},n} \mathcal{G}_{\vec{r}}(\alpha, \beta, t_{0,n}, t'') R_{\vec{r}}(t' - t'', T_{\vec{r}}) \right]$$

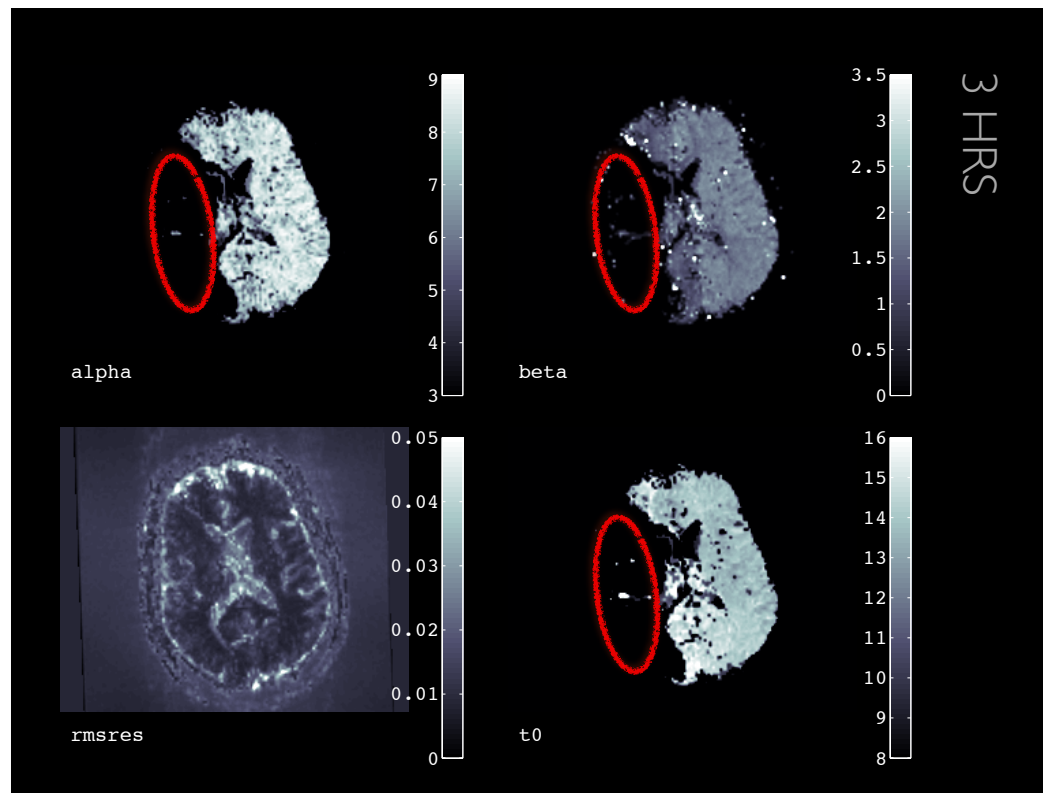
BAYESIAN ANALYSIS

- Priors for parameters factored into independent, physiologically consistent Gaussians
- Marginalized likelihoods from Jeffreys' priors
- Joint posterior probabilities estimated with simulated annealing, Markov-chain Monte Carlo, Metropolis-Hastings sampling

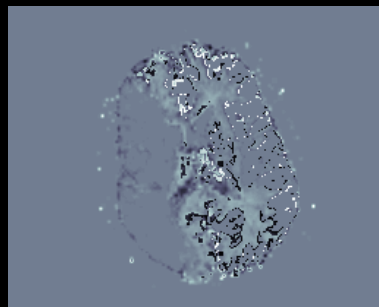
Lee, et al. Magn. Res. Med. 63:1305–1314 (2010)

Shimony, et al. Bayesian Inf. & Max. Ent. Methods in Sci. & Eng. 55:805-815 (2006)

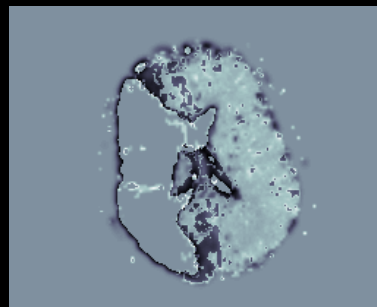




3 HRS



$\text{std_mom}(F) - \text{std_mom}(CBF)$



$\text{std_mom}(T) - \text{std_mom}(MTT)$

CASE 7377

Chronic moyamoya disease in a 45 YO male with minimal symptoms.

Enrolled in RO1 NS051631-04.

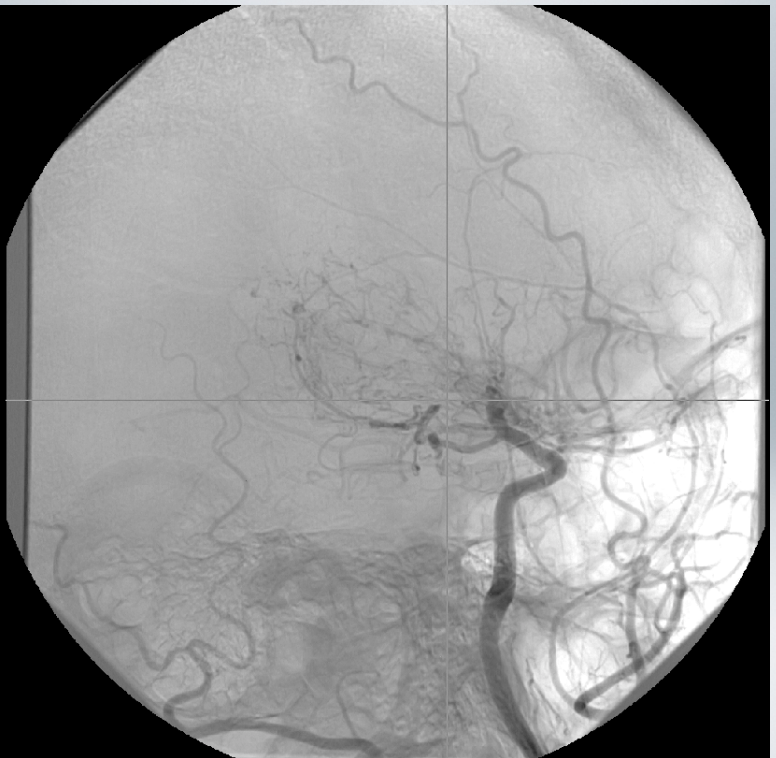
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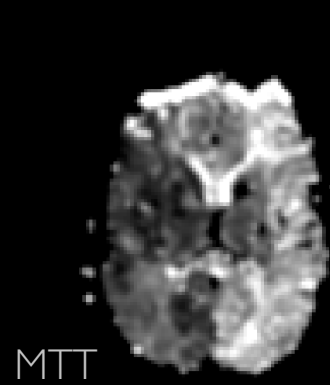
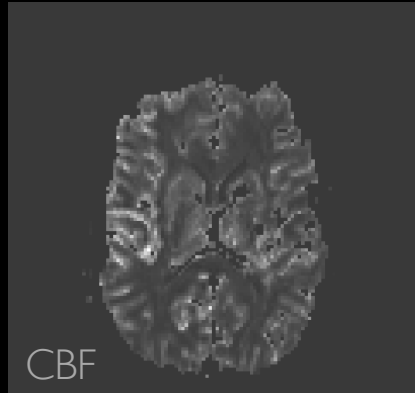
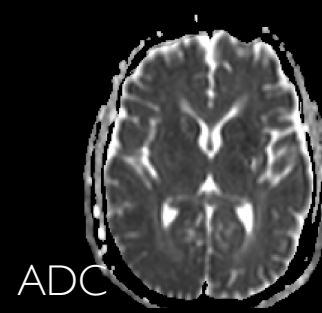
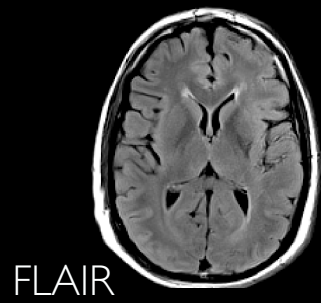


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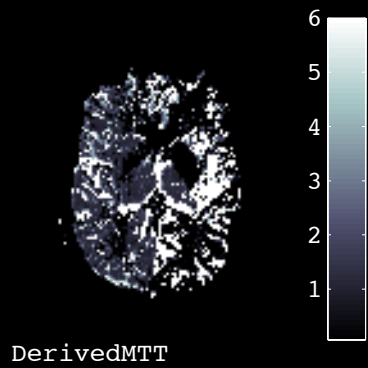
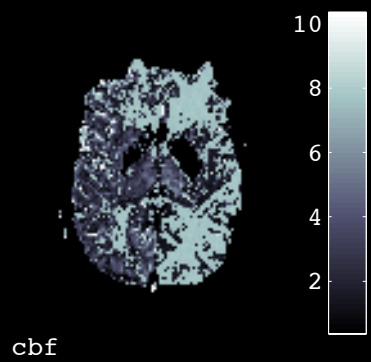
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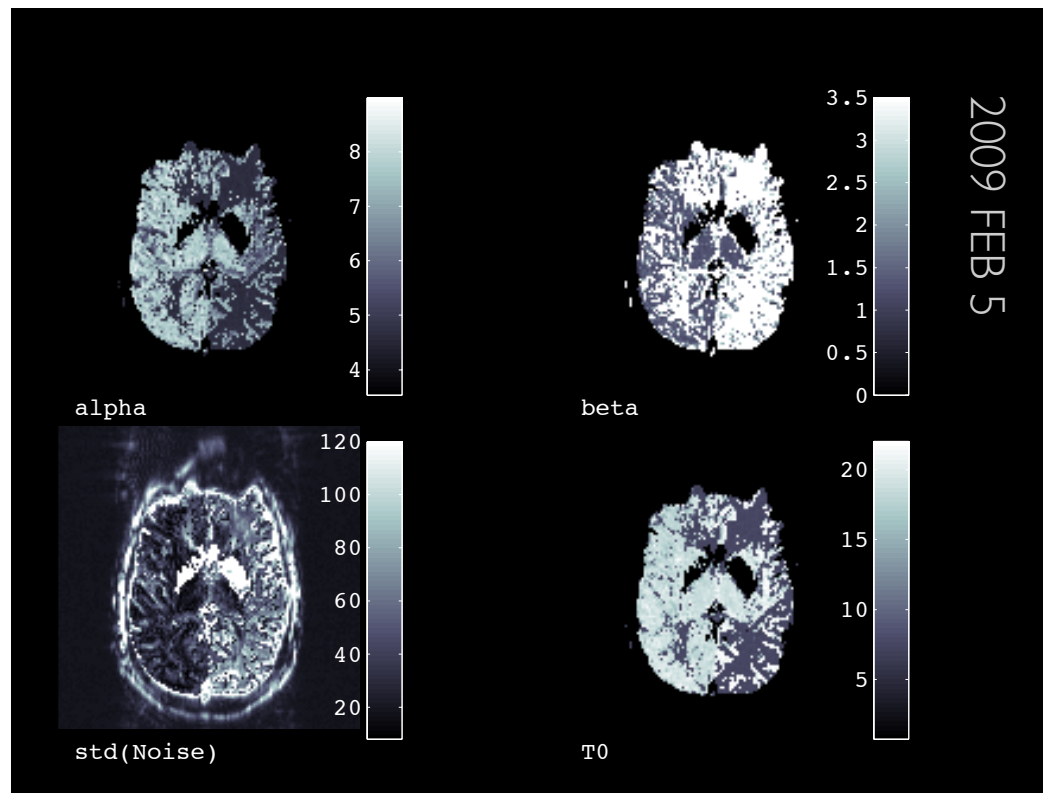


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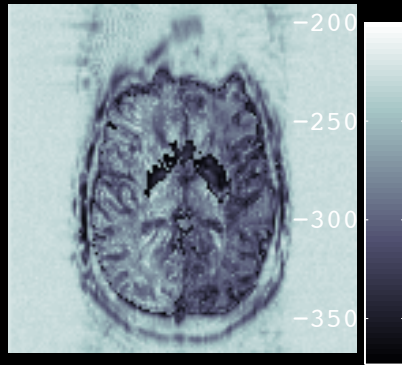


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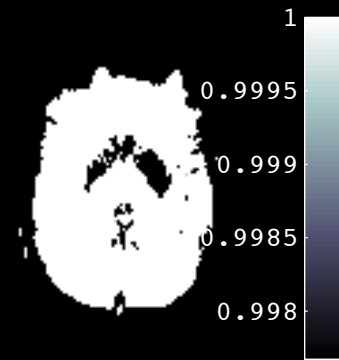




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ProbModel

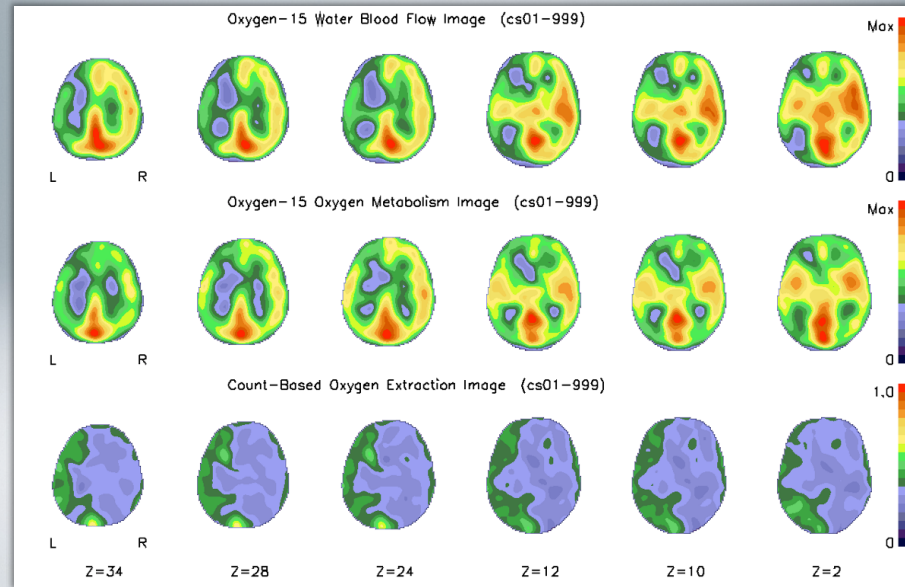


ProbSignal

PET

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COMPUTATION

IBM e1350 Cluster: 7x x3950 M2 SMP nodes, 16 quad core 2.4 GHz Xeon E7440 ea.,
448 cores, < 17 Tflops total

Qlogic 9240, DDR 288-port **Infiniband Switch**; 8000F GigE leaf & 8000R GigE aggregation switches

Management, Login, Gateway, General Parallel Filesystem: 9x x3650 M2 nodes, dual quad core Xeon L5520, Mellanox ConnectX 2-port, 4x DDR HCA, 4 Gb HBA ea.

DS4700 **storage controller:** 3x DS4000 EXP810 expansions

Pending: IBM iDataPlex Cluster: 168x dx360 M2 nodes, dual quad core 2.66 GHz Xeon X5550 (Nehalem-EP) ea., **1344 cores, < 57 Tflops** total

Single-model analysis, single perfusion-weighted EPI study:

~10¹⁷ flop, ~30 min

LARRY'S MCMC

<http://bayesiananalysis.wustl.edu>

NEXT STEPS?

- Evidence (marginal likelihood, marginal density of data, prior predictive, viz., $Z = \int L(\theta)\pi(\theta)d\theta$)
- More informative priors: clinical information?
- Oxygen metabolism

SUMMARY

MR evaluations of stroke have been unable to predict clinical outcomes.

Bayesian inference provides new models & metrics that may improve evaluation of stroke patients

Clinical trials are underway

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Acute Stroke Chronic Stroke MR, PET & Analysis

Hongyu An	Colin Derdeyn	Hongyu An	Lennis Lich
Andria Ford	Nancy Hantler	Jeffrey Baumstark	Mark Nolte
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